#### Mathematics 3201 Unit 6: Exponential Functions Unit Assessment

# Name:\_\_\_\_\_

D) 3

# Section 1: Selected Response (32 points) Circle the letter of the correct answer.

| 1.<br>A) f        | Which represents<br>$f(x) = \frac{1}{3} \left(\frac{4}{5}\right)^{x}$ |                                  |  | C)     | f(x) = 2(1        | ) <sup>x</sup> | D) | $f(x) = \frac{1}{2}(3)^x$ |
|-------------------|---|----------------------------------|--|--------|-------------------|----------------|----|---------------------------|
| 2.<br>A)          | What is the y-inte (0, 2)   | rcept of:<br>B) (0, 5            |  | C)     | (0, 10)           |                | D) | (0, 0)                    |
| 3.<br>A) <i>f</i> | Which exponentia $T(x) = 4(2)^x$                                      | l function C) $f(x)$             | •  | grapl  | n shown?          |                |    |                           |
| <b>B)</b> ;       | $f(x) = 4\left(\frac{1}{2}\right)^x$                                  | D) <i>f</i> (x) =                | $=3\left(\frac{1}{2}\right)^{x}$             |        |                   |                |    | -2 2 4 6 8 10 X           |
| 4.                | What is the range   | of $f(x) =$                      | 4(3) <sup>x</sup> ?                          |        |                   |                |    |                           |
| A)                | <i>y</i> > 4  | B) <i>y</i> ≥                    | 4  | C)     | <i>y</i> > 0      |                | D) | $y \ge 0$                 |
| 5.                | What is the doma  | in of f(x)                       | $=\frac{1}{2}\left(\frac{3}{4}\right)^{x}$ ? |        |                   |                |    |                           |
|                   | $x \ge \frac{1}{2}$   | B) $x \in R$                     | - (1)  | C)     | $x > \frac{3}{4}$ |                | D) | x > 0                     |
| 6.                | What is the expor   | nential fun                      | ction for the dat                            | ta giv | /en:              |                |    |                           |
|                   | x -1  |                                  | 0  | 1      |                   | 2              |    | 3                         |
|                   | f(x) 81   |                                  | 27   | 9      |                   | 3              |    | 1                         |
| <b>A)</b> ;       | $f(x) = 27 \left(\frac{1}{3}\right)^x$                                | B) <i>f</i> ( <i>x</i> )         | $=81\left(\frac{1}{3}\right)^{x}$            | C)     | f(x) = 27         | $(3)^{x}$      | D) | $f(x) = 81(3)^x$          |
| 7.<br>A)          | Solve for x: $\frac{1}{8}$  | $5^{2x+1} =$<br>B) $\frac{1}{7}$ |  | C)     | $\frac{1}{4}$     |                | D) | 7                         |
| 8.<br>A)          | Solve for x: $\frac{1}{4}$  | $2^{3x} = \sqrt{B}$              |  | C)     | 1                 |                | D) | 2                         |
| 9.                | What is the value   | of x if f(x                      | ) in the equatior                            | n 81   | $=3^{-3(x+2)}$    |                |    |                           |

B)  $\frac{-2}{3}$  C)  $\frac{3}{5}$ 

A)  $\frac{-10}{3}$ 

### 10. What is the true of the table given below?

| -         |    |    |    |     |     |
|-----------|----|----|----|-----|-----|
| x(years)  | 0  | 2  | 4  | 6   | 8   |
| y(amount) | 10 | 30 | 90 | 270 | 810 |

|    | Initial Amount | Amount Growth             |
|----|----------------|---------------------------|
| A) | 10             | doubles every three years |
| B) | 10             | triples every two years   |
| C) | 20             | doubles every three years |
| D) | 20             | triples every two years   |

- 11. The function that models the decay of carbon-14 is  $A(t) = 50 \left(\frac{1}{2}\right)^{\frac{t}{5730}}$  where A(t) is the number of grams of carbon-14 present at time t, in years. Which statement is true?
  - A) The amount of carbon-14 doubles every 5730 years.
  - B) There are 100 g of carbon-14 present initially.
  - C) 25 g will be present after 50 years.
  - D) 25 g of carbon-14 will be present after 5730 years.

12.  $A = 1000(1.09)^4$  represents a bank loan that is compound annually. What is the interest rate?

| A) | 1000% | B) | 9% | C) 81% | D) 4% |
|----|-------|----|----|--------|-------|
|----|-------|----|----|--------|-------|

13. Rick's car valued at \$22,600 depreciates in value by 16% per year. Which equation represents the car's value after 5 years?

A)  $V = 22600(1.16)^5$  B)  $V = 22600(0.16)^5$  C)  $V = 22600(0.84)^5$  D)  $V = 22600(1.84)^5$ 

14. Joel invested \$5000 in a savings account that pays 6%/a compounded quarterly. Which equation represents how much money Joel has after 6 years?

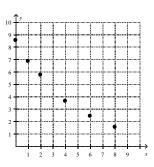
A)  $V = 5000(1.05)^6$  B)  $V = 5000(1.025)^6$  C)  $V = 5000(1.0125)^6$  D)  $V = 5000(1.004)^6$ 

#### 15. The following data shows exponential growth. Determine the missing value in the given table.

|                        | /  |
|------------------------|----|
| y 3 6 12 24 48 x 192 3 | 84 |

A) 72 B) 96 C) 104 D) 144

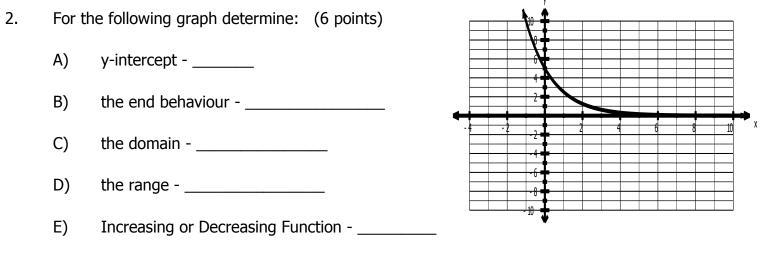
- 16. A scatter plot is drawn using a data set. Identify the equation of the curve of best fit.
- A)  $f(x) = 4.8(1.08)^x$  C)  $f(x) = 8.4(0.81)^x$
- B)  $f(x) = 4.8(0.81)^x$  D)  $f(x) = 8.4(1.08)^x$



# Section 2: Constructed Response (40 points) Answer all the questions showing all your work.

1. Complete the table below: (12 points)

| Characteristics             | $f(x) = 5^x$ | $f(x) = 3(2)^x$ | $f(x) = \left(\frac{1}{2}\right)^x$ | $f(x) = 4\left(\frac{1}{3}\right)^x$ |
|-----------------------------|--------------|-----------------|-------------------------------------|--------------------------------------|
| Number of x-<br>intercepts  |              |                 |                                     |                                      |
| y-intercept                 |              |                 |                                     |                                      |
| End Behaviour               |              |                 |                                     |                                      |
| Domain                      |              |                 |                                     |                                      |
| Range                       |              |                 |                                     |                                      |
| Increasing or<br>Decreasing |              |                 |                                     |                                      |



Is the parameter "b" in the equation of the function greater than 1 or between 0 and 1? F) Provide your reasoning.

Solve each exponential equation. (12 marks) 3.

 $n^{r+1}$ /22

| A) | $2(3)^{x} = 54$ | B) $2^{x+1} = \sqrt{32}$ |
|----|-----------------|--------------------------|
|    |                 |                          |
|    |                 |                          |
|    |                 |                          |
|    |                 |                          |
|    |                 |                          |
|    |                 |                          |

| C) $25^{(x-3)} = \frac{1}{125}$ | D) $2\left(\frac{1}{3}\right)^{2x} = 18$ |
|---------------------------------|--|
|                                 |  |
|                                 |  |
|                                 |  |
|                                 |  |
|                                 |  |

- 4. Joanne invested \$5000 in a savings account that pays 7% per year compounded quarterly.A) Write an equation to represent the above situation. (3 points)
  - B) How much money will Joanne have after 2 years? (2 points)

- 5. Samuel's car currently valued at \$32000, depreciates in value by 18% per year.A) Write an equation to represent the above situation. (3 points)
  - B) What will the car be worth in 4 years? (2 points)