# Mathematics 3201 <br> Unit 6: Exponential Functions <br> Unit Assessment 

## Name:

$\qquad$

## Section 1: Selected Response (32 points) Circle the letter of the correct answer.

1. Which represents an increasing function?
A) $\mathrm{f}(\mathrm{x})=\frac{1}{3}\left(\frac{4}{5}\right)^{x}$
B) $\mathrm{f}(\mathrm{x})=2\left(\frac{2}{3}\right)^{x}$
C) $f(x)=2(1)^{x}$
D) $f(x)=\frac{1}{2}(3)^{x}$
2. What is the $y$-intercept of: $f(x)=5(2)^{x}$ ?
A) $(0,2)$
B) $(0,5)$
C) $(0,10)$
D) $(0,0)$
3. Which exponential function represents the graph shown?
A) $f(x)=4(2)^{x}$
B) $f(x)=4\left(\frac{1}{2}\right)^{x}$
C) $f(x)=2(4)^{x}$
D) $f(x)=3\left(\frac{1}{2}\right)^{x}$
4. What is the range of $f(x)=4(3)^{x}$ ?

A) $y>4$
B) $y \geq 4$
C) $y>0$
D) $y \geq 0$
5. What is the domain of $\mathrm{f}(\mathrm{x})=\frac{1}{2}\left(\frac{3}{4}\right)^{x}$ ?
A) $x \geq \frac{1}{2}$
B) $x \in R$
C) $x>\frac{3}{4}$
D) $x>0$
6. What is the exponential function for the data given:

| $x$ | -1 | 0 | 1 | 2 | 3 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| $f(x)$ | 81 | 27 | 9 | 3 | 1 |

A) $f(x)=27\left(\frac{1}{3}\right)^{x}$
B) $f(x)=81\left(\frac{1}{3}\right)^{x}$
C) $f(x)=27(3)^{x}$
D) $f(x)=81(3)^{x}$
7. Solve for x : $\quad 5^{2 x+1}=125^{3 \mathrm{x}}$
A) $\frac{1}{8}$
B) $\frac{1}{7}$
C) $\frac{1}{4}$
D) 7
8. Solve for $x$ :
$2^{3 x}=\sqrt{4}^{x+1}$
A) $\frac{1}{4}$
B) $\frac{1}{2}$
C) 1
D) 2
9. What is the value of $x$ if $f(x)$ in the equation $81=3^{-3(x+2)}$
A) $\frac{-10}{3}$
B) $\frac{-2}{3}$
C) $\frac{3}{5}$
D) 3
10. What is the true of the table given below?

| $x$ (years) | 0 | 2 | 4 | 6 | 8 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| $y$ (amount) | 10 | 30 | 90 | 270 | 810 |


|  | Initial Amount | Amount Growth |
| :---: | :---: | :---: |
|  | 10 | doubles every three years |
| B) | 10 | triples every two years |
| C) | 20 | doubles every three years |
| D) | 20 | triples every two years |

11. The function that models the decay of carbon-14 is $A(t)=50\left(\frac{1}{2}\right)^{\frac{t}{5730}}$ where $A(t)$ is the number of grams of carbon-14 present at time $t$, in years. Which statement is true?
A) The amount of carbon-14 doubles every 5730 years.
B) There are 100 g of carbon-14 present initially.
C) $\quad 25 \mathrm{~g}$ will be present after 50 years.
D) 25 g of carbon-14 will be present after 5730 years.
12. $A=1000(1.09)^{4}$ represents a bank loan that is compound annually. What is the interest rate?
A) $1000 \%$
B) $9 \%$
C) $81 \%$
D) $4 \%$
13. Rick's car valued at $\$ 22,600$ depreciates in value by $16 \%$ per year. Which equation represents the car's value after 5 years?
A) $V=22600(1.16)^{5}$
B) $V=22600(0.16)^{5}$
C) $V=22600(0.84)^{5}$
D) $\quad V=22600(1.84)^{5}$
14. Joel invested $\$ 5000$ in a savings account that pays $6 \% / a$ compounded quarterly. Which equation represents how much money Joel has after 6 years?
A) $V=5000(1.05)^{6}$
B) $\quad V=5000(1.025)^{6}$
C) $V=5000(1.0125)^{6}$
D) $\quad V=5000(1.004)^{6}$
15. The following data shows exponential growth. Determine the missing value in the given table.

| $x$ | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $y$ | 3 | 6 | 12 | 24 | 48 | $x$ | 192 | 384 |

A) 72
B) 96
C) 104
D) 144
16. A scatter plot is drawn using a data set. Identify the equation of the curve of best fit.
A) $f(x)=4.8(1.08)^{x}$
B) $f(x)=4.8(0.81)^{x}$
C) $f(x)=8.4(0.81)^{x}$
D) $f(x)=8.4(1.08)^{x}$


## Section 2: Constructed Response (40 points) <br> Answer all the questions showing all your work.

1. Complete the table below: (12 points)

| Characteristics | $\mathrm{f}(\mathrm{x})=5^{\mathrm{x}}$ | $\mathrm{f}(\mathrm{x})=3(2)^{\mathrm{x}}$ | $f(x)=\left(\frac{1}{2}\right)^{x}$ | $f(x)=4\left(\frac{1}{3}\right)^{x}$ |
| :--- | :--- | :--- | :--- | :--- |
| Number of $\mathrm{x}-$ <br> intercepts |  |  |  |  |
| y -intercept |  |  |  |  |
| End Behaviour |  |  |  |  |
| Domain |  |  |  |  |
| Range |  |  |  |  |
| Increasing or <br> Decreasing |  |  |  |  |

2. For the following graph determine: (6 points)
A) $y$-intercept - $\qquad$
B) the end behaviour - $\qquad$
C) the domain - $\qquad$
D) the range - $\qquad$

E) Increasing or Decreasing Function - $\qquad$
F) Is the parameter " $b$ " in the equation of the function greater than 1 or between 0 and 1 ? Provide your reasoning.
3. Solve each exponential equation. (12 marks)

| A) $2(3)^{x}=54$ | B) $2^{x+1}=\sqrt{32}$ |
| :--- | :--- |
|  |  |


| C) $25^{(x-3)}=\frac{1}{125}$ | D) $2\left(\frac{1}{3}\right)^{2 x}=18$ |
| :--- | :--- |
|  |  |

4. Joanne invested $\$ 5000$ in a savings account that pays $7 \%$ per year compounded quarterly. A) Write an equation to represent the above situation. (3 points)
B) How much money will Joanne have after 2 years? (2 points)
5. Samuel's car currently valued at $\$ 32000$, depreciates in value by $18 \%$ per year.
A) Write an equation to represent the above situation. (3 points)
B) What will the car be worth in 4 years? (2 points)
