

Mathematics 3200 Test  
Chapter 4: Trigonometry and The Unit Circle

40

NAME: \_\_\_\_\_

SECTION A: Place the LETTER of your response in the space at the right.

13 pts

1. Convert  $160^\circ$  to radians. 1. \_\_\_\_\_
- A  $\frac{9\pi}{16}$
- B  $\frac{9\pi}{8}$
- C  $\frac{8\pi}{9}$
- D  $\frac{5\pi}{6}$
2. If  $\theta$  is a standard position angle measuring 8 rad, in which quadrant does the terminal arm of  $\theta$  lie? 2. \_\_\_\_\_
- A Quadrant I
- B Quadrant II
- C Quadrant III
- D Quadrant IV
3. Which best approximates the value of  $\cot(200^\circ) + \csc(3)$ ? 3. \_\_\_\_\_
- A 0.3273
- B 1.7374
- C 9.8336
- D 21.8548
4. If  $\cot(\theta) < 0$  and  $\sec(\theta) > 0$ , in which quadrant does the terminal arm of angle  $\theta$  lie? 4. \_\_\_\_\_
- A Quadrant I
- B Quadrant II
- C Quadrant III
- D Quadrant IV
5. Solve:  $\csc(x) + 2 = 0$ , where  $0 \leq x \leq \pi$  5. \_\_\_\_\_
- A  $x = \frac{\pi}{3}$
- B  $x = \frac{\pi}{6}$
- C  $x = \frac{\pi}{3}, x = \frac{2\pi}{3}$
- D  $x = \frac{\pi}{6}, x = \frac{5\pi}{6}$

6. If  $\beta$  is an angle in standard position with  $\csc(\beta) = -\frac{25}{7}$  and  $\tan(\beta) > 0$ , which is true for  $\sec(\beta)$  and the measure of  $\beta$ ? 6.\_\_\_\_\_

A  $\sec(\beta) = -\frac{25}{24}, \quad \beta = 196^\circ$

B  $\sec(\beta) = \frac{25}{24}, \quad \beta = 16^\circ$

C  $\sec(\beta) = -\frac{25}{24}, \quad \beta = 344^\circ$

D  $\sec(\beta) = \frac{25}{24}, \quad \beta = 164^\circ$

7. Solve:  $\csc^2(\alpha) = 1$ , where  $\alpha \in [0, 2\pi)$  7.\_\_\_\_\_

A  $\alpha = \frac{\pi}{2}$

B  $\alpha = \frac{\pi}{2}, \alpha = \frac{3\pi}{2}$

C  $\alpha = 0$

D  $\alpha = 0, \alpha = \pi$

8. A circle centered at the origin contains the point  $(-12, 16)$ . What is the equation of this circle? 8.\_\_\_\_\_

A  $x^2 + y^2 = 16$

B  $x^2 + y^2 = 20$

C  $x^2 + y^2 = 40$

D  $x^2 + y^2 = 400$

9. What is the length of the arc intercepted by a central angle of  $100^\circ$  in a circle with radius 4.6 cm? 9.\_\_\_\_\_

A 1.28 cm

B 4.01 cm

C 6.92 cm

D 8.03 cm

10. Which pair of angles is coterminal? 10.\_\_\_\_\_

A  $\frac{5\pi}{3}$  and  $-\frac{5\pi}{3}$

B  $-\frac{\pi}{3}$  and  $\frac{2\pi}{3}$

C  $\frac{5\pi}{6}$  and  $-\frac{7\pi}{6}$

D  $\frac{2\pi}{3}$  and  $\frac{4\pi}{3}$

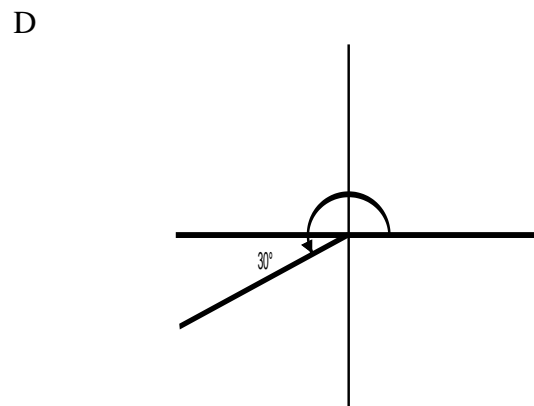
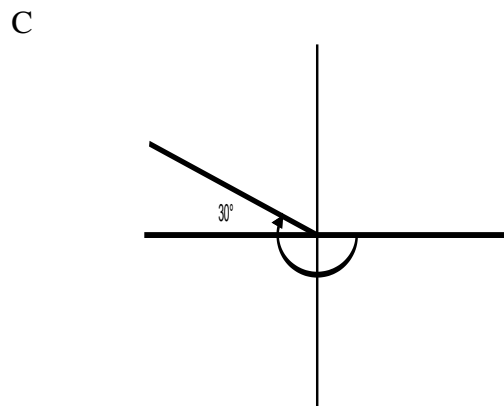
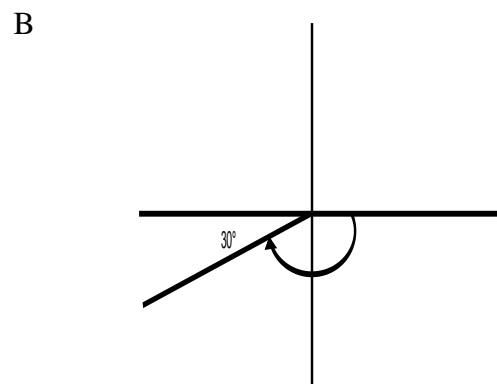
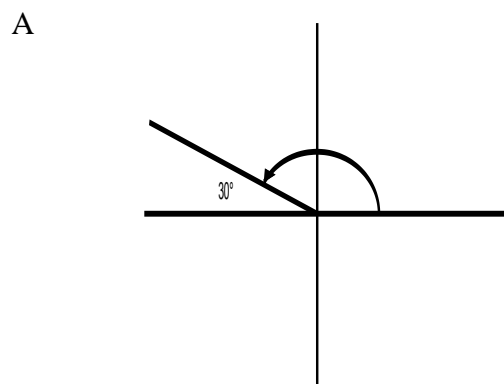
11. What is the exact value of  $\tan(30^\circ) + \cot(30^\circ)$

11. \_\_\_\_\_

- A 1
- B  $\frac{4\sqrt{3}}{3}$
- C  $\frac{2\sqrt{3}}{3}$
- D  $\sqrt{3}$

12. Which represents an angle measuring  $\frac{7\pi}{6}$  ?

12. \_\_\_\_\_



13. Which of the following points lies on the unit circle?

13. \_\_\_\_\_

- A  $\left(\frac{\sqrt{3}}{2}, -\frac{\sqrt{3}}{2}\right)$
- B  $\left(\frac{1}{2}, \frac{1}{2}\right)$
- C  $\left(\frac{3}{5}, -\frac{4}{5}\right)$
- D  $\left(\frac{2}{3}, \frac{1}{3}\right)$

SECTION B: Answer ALL questions in the space provided. Full credit will only be awarded for correct solutions that include relevant workings.

- 1 The point  $(-4, 8)$  lies on the terminal arm of an angle,  $\theta$ , in standard position. Sketch the angle in standard position. Determine the exact value, in simplest radical form, for all six trigonometric ratios of  $\theta$ . Calculate the measure of the reference angle, and determine the measure of  $\theta$ . 6 pts

2. Determine the EXACT value, in simplest form, for  $\frac{\sin\left(-\frac{4\pi}{3}\right) + \sec\left(\frac{\pi}{4}\right)}{\tan(-120^\circ)}$  4 pts

3. Determine the general solution to the equation below, where  $x$  is in degrees. 6 pts
- $$6\tan^2(x) - \tan(x) - 15 = 0$$

4. Solve for  $x$ , where  $-\pi \leq x < 2\pi$        $\sec^2(x) = 3\sec(x) - 2$       6 pts

5. On a circle with radius 6 cm, two points are described as follows:      5 pts

Point A is determined by rotating the point  $(6,0)$  through an angle of 3 radians.

Point B is determined by rotating the point  $(0, -6)$  through an angle of  $-210^\circ$ .

What is the length of the longer arc joining A and B?