Math 3200 Exam 1 Unit 2 Transformations of Functions Name:

Circle the correct response. 2 marks each

 The graph y = f(x) contains the point (3, 4). After a transformation, the point (3, 4) is transformed to (5, 5). Which of the following is a possible equation of the transformed function?

A y + 1 = f(x + 2)B y + 1 = f(x - 2)C y - 1 = f(x + 2)D y - 1 = f(x - 2)

- 2. The graph of y = |x| is transformed by a vertical stretch by a factor of 3 about the x-axis, and then a horizontal translation of 3 units left and a vertical translation up 1 unit. Which of the following points is on the transformed function?
 - **A** (0, 0) **B** (1, 3)
 - C (-3, 1)
 - **D** (3, 1)
- 3. The graph of $y = \sqrt{x}$ is vertically stretched by a factor of 2 about the *x*-axis, then reflected about the *y*-axis, and then horizontally translated left 3. What is the equation of the transformed function?

A
$$y = 2\sqrt{-x-3}$$

B $y = 2\sqrt{-x+3}$
C $y = -2\sqrt{x+3}$
D $y = -2\sqrt{x-3}$

4. Which of the following transformations would produce a graph with the same *x*-intercepts as y = f(x)?

A
$$y = -f(x)$$

B $y = f(-x)$
C $y = f(x + 1)$
D $y = f(x) + 1$

5. Given the graph of y = f(x), what is the invariant point under the transformation y = f(-2x)?



- 6. What will the transformation of the graph of y = f(x) be if y is replaced with -y in the equation y = f(x)?
 - A It will be reflected in the x-axis.
 - B It will be reflected in the y-axis.
 - **C** It will be reflected in the line y = x.
 - **D** It will be reflected in the line y = -1.
- 7 When the value of a is less than -1, the function $g(x) = ax^2$ has what relationship to the base function $f(x) = x^2$?
 - A f(x) is compressed vertically
 - **B** f(x) is reflected and compressed vertically
 - $\mathbf{C} = f(x)$ is stretched vertically
 - **D** f(x) is reflected and stretched vertically
- 8 Which choice best describes the combination of transformations that must be applied to the graph of f(x) = |x| to obtain the graph of g(x) = f(2x 4)?
 - ${\bf A}_{-}$ a horizontal stretch by a factor of 2 and a horizontal translation of 2 units to the left
 - **B** a horizontal stretch by a factor of $\frac{1}{2}$ and a horizontal translation of 4 units to the right
 - **C** a horizontal stretch by a factor of $\frac{1}{2}$ and a horizontal translation of 2 units to the right
 - \mathbf{D} a horizontal stretch by a factor of -2 and a horizontal translation of 2 units to the right

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Which of the following functions is the correct inverse for the function $f(x) = -\frac{9}{2}x + 6$?

A $f^{-1}(x) = -\frac{2}{9}x + \frac{4}{3}$ B $f^{-1}(x) = \frac{9}{2}x + \frac{4}{3}$ C $f^{-1}(x) = -\frac{2}{9}x - \frac{4}{3}$ D $f^{-1}(x) = \frac{9}{2}x - \frac{4}{3}$ 10 Which graph represents the inverse of the function shown?



11 If y = f(x) is transformed by the transformation, y - 6 = -4f(-2x + 8), which statement below is true?

A) f(x) is transformed 8 units left, 6 units down with a horizontal stretch of -2 and a vertical stretch of -4

B) f(x) is transformed 8 units left, 6 units up with a horizontal stretch of $\frac{1}{2}$ and a vertical

stretch of $\frac{1}{4}$

C) f(x) is transformed 4 units left, 6 units up with a horizontal stretch of $\frac{1}{2}$ and a vertical stretch of 4

D) f(x) is transformed 4 units right, 6 units up with a horizontal stretch of .5 and a vertical stretch of 4, reflected in the x axis.

- 12 What would be the mapping rule for the transformation performed in question 11?
 - A) $(x, y) \rightarrow (-.5x 8, 6y 4)$ B) $(x, y) \rightarrow (-.5x - 8, -4y + 6)$ C) $(x, y) \rightarrow (-.5x + 4, -4y - 6)$ D) $(x, y) \rightarrow (-.5x + 4, -4y + 6)$

Part II

1) Given the graph of y = f(x) below, sketch the graph of the transformation y = -2f(-2(x - 4)) + 1 by using a table of values for the key points of y = f(x) and a mapping rule. 10 marks



2) Given the sketch of y = f(x) below, y = g(x) is a transformation of y = f(x). Determine the equation of the transformation in the form y = af(b(x-h))+k algebraically. Be sure to show all workings. 10 marks



3 Given $y = x^2 - 4x + 1$,

A) determine the equation of the inverse. 6 marks

- B) Restrict the domain of y=f(x) above and write the equation of the inverse now. 3 marks
- C) Use a table of values along with your restricted domain in B to sketch the graphs of y = f(x) and $y = f^{-1}(x)$ on the same x-y plane with the mirror y = x. 8 marks

